Index No.	
Medium	ENGLISH

SRI LANKAN MATHEMATICS COMPETITION 8 - 2019

September 28, 2019 10:30 am – 12 noon

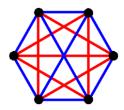
This question paper has **30 multiple choice questions**. The duration of this competition is **90 minutes**. **Answer all questions**. Please read the questions carefully and **fill in the correct lettered circle (only one) against the correct question number in the given answer sheet**. Note that no responses get at least two points while incorrect responses receive zero points. **Please write your index number in the box provided at the top right corner of your question paper**.

Scoring System for the Sri Lankan Mathematics Competition 8

Questions 1 to 10: 5 points for correct response, 2 points for no response, and 0 points for incorrect response.

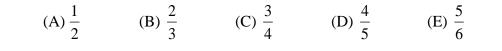
Questions 11 to 20: 6 points for correct response, 2 points for no response, and 0 points for incorrect response.

Questions 21 to 30: 8 points for correct response, 3 points for no response, and 0 points for incorrect response.

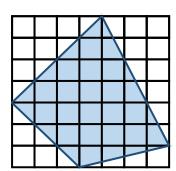


Sri Lanka Olympiad Mathematics Foundation

1. Which of the following numbers is closest in value to 2.019×2.718 ? (B) 60(C) 600(D) 6000 (E) 60000 (A)62. 1000000000-888888887 is equal to (B) 111 111 112 (A) 111 111 111 (C) 111 111 113 (E) 222 222 223 (D) 222 222 221 3. When 111 111 111 is divided by 111, how many digits are there in the quotient? (C) 8 (D) 10 (E) 12 (A)4(B) 64. Which fraction is the largest?



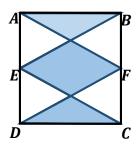
5. In the square grid shown below, each small square has area 1 cm². What is the area of the shaded region in cm²?



- (A) 23.5 (B) 24 (C) 24.5 (D) 25 (E) 25.5
- 6. When 5^{-4} is written as a terminating decimal, what is the sum of its digits?
 - (A) 5 (B) 6 (C) 7 (D) 8 (E) 9
- 7. What is the percentage of square numbers among the whole numbers from 1 to 100 inclusive of 1 and 100?
 - (A) 7% (B) 8% (C) 9% (D) 10% (E) 11%

- 8. What is the 2019th number in the sequence of numbers $\frac{3}{4}$, $\frac{4}{5}$, $\frac{5}{6}$, $\frac{6}{7}$,...?

- (A) $\frac{2019}{2020}$ (B) $\frac{2020}{2021}$ (C) $\frac{2021}{2022}$ (D) $\frac{2022}{2023}$ (E) $\frac{2023}{2024}$
- 9. What is the smallest number that can be made by using each digit 2, 0, 1 and 9 of 2019 exactly once and the operations addition and/or multiplication any number of times?
 - (A)0
- (B) 1
- (C) 2
- (D)3
- (E)9
- 10. ABCD is a rectangle and E and F are midpoints of AD and BC respectively.

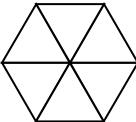


What is the ratio, area of shaded region to area of unshaded region?

- (A)1:1
- (B) 1:2
- (C) 2:1
- (D) 1:4
- (E) 4:1
- 11. A box has a certain number of mangoes. Sarath, Adul, Meena, Kamala and Susan guessed that the numbers of mangoes is 33, 32, 30, 28 and 27 respectively. If only one guess is correct and two guesses differ by 2 from the actual number and two guesses differ by 3 from the actual number, then who guessed correctly?
 - (A) Sarath
- (B) Abdul
- (C) Meena
- (D) Kamala
- (E) Susan

- 12. What is the units digit of 9^{2019} ?
 - (A)1
- (B) 2
- (C)3
- (D) 4
- (E) 9
- 13. How many digits does the number (111 111 111)² have?
 - (A)9
- (B) 16
- (C) 17
- (D) 18
- (E) 20
- 14. The product $100 \times 101 \times 102$ is not divisible by
 - (A)2
- (B) 3
- (C) 5
- (D) 17
- (E) 103

15. The figure given below contains 6 equilateral triangles. How many rhombuses does it contain?



- (A)6
- (B) 8
- (C) 10
- (D) 12
- (E) 14
- 16. How many different pairs of integers (a,b) satisfy $a^b = 81$?
 - (A)1
- (B) 2
- (C) 3
- (D) 4
- (E) 5
- 17. The product of 2019 integers is equal to 1. Their sum cannot be equal to
 - (A) 9
- (B) -1
- (C) 2
- (D) 3
- (E)7
- 18. Martians use a positional number system with a base different from 10. A correct addition problem in their system is shown below using our Hindu-Arabic numerals:

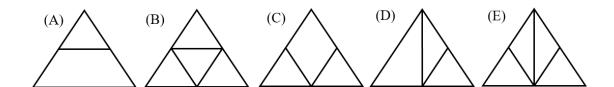
$$\begin{array}{r} 4421 \\ + 1154 \\ \hline 5605 \end{array}$$

- What is their base?
- (A)4
- (B)5
- (C) 6
- (D) 7
- (E) 8
- 19. How many different positive divisors does 72 have?
 - (A)8
- (B) 9
- (C) 10
- (D) 11
- (E) 12
- 20. In how many ways can a path starting from the box containing S and ending in a box containing the number 8 be traversed through boxes containing S, L, M, C, and 8 in that order if the path consists of horizontal and/or diagonally down straight line segments connecting a pair of neighboring (a box can have at most 8 neighbors above, below, left, right and diagonal) boxes?

S	L	M	C	8
	L	M	C	8
		M	C	8
			C	8
				8

	, Abdul, Kamal, Sar amil New Year Fo			•	
	ring before the race:	ostivai ana iiai	man, Tamar	a, Weena and Sa	sair sair
Hanna	h: Sarath or Abdul	will win.			
	la: Sanjeeva or Anw				
	a: Sarath or Sanjeeva				
	: Sanjeeva or Abdul one of them was righ		race?		
Omy	me of them was rigi	it. Who won the	race:		
(A)Sa	rath (B) Abdul	(C) Kamal	(D) Sanje	eva (E) Anwar	
22. Little	Nimal has to distri	bute 4 hats co	lored red, bl	ue, green and vell	low to
	s Kamal, Sanjeeva,			•	
green	and yellow respecti	vely. In how m	any ways ca	n Nimal distribute	hats so
only o	ne gets his or her far	vorite colored h	at?		
(A)0	(B) 1	(C) 2	(D) 3	(E) 8	
23 Consid	der the following sta	itements:			
	athematicians like th				
	litician is logical.				
-	al people do not like	e the color red.			
Which	of the following is/	are valid conclu	sions?		
I.	Politicians do not l				
II.	Some politicians li				
III.	Illogical people are	e not mathemati	cians.		
(A) I o	only (B) II only	(C) III only	(D) I and	III only (E) II	and III
24 For no	ositive real numbers	a and h dafina	$a \otimes b = a \times b$	b y	oro ore
24. Por po	ositive rear numbers	a and b , define	$a \otimes b = \frac{a}{a+a}$	b where x and +	are ore
multip	olication and additio	n respectively.	How many d	ifferent pairs of in	tegers
satisfy	$a \otimes b = 1$?				
(A)0	(B) 1	(C) 2	(D) 3	(E) 4	
25. A sup	ermarket has 50 b	_			
	C 50	and 60 1111 '	. 41 1		
	bes inclusive of 50				there
	bes inclusive of 50 boxes containing the				there
	boxes containing th				there

26. Which figure cannot be drawn without lifting the pencil and without going over a straight line segment again?



- 27. Sarath and Meena play a game in which they take turns in adding a positive integer less than the current number to the current number. They start with 2. The player who reaches 100 first wins the game. Which of the following is/are true?
 - I. The player who plays first (first player) has a winning strategy.
 - II. First player can always win in the 5th move.
 - III. The player who plays second (second player) has a winning strategy if the game starts with 3.
 - $\text{(A) I only} \qquad \text{(B) II only} \qquad \text{(C) III only} \qquad \text{(D) I and III only} \qquad \text{(E) All}$
- 28. *A* is the collection of positive integers that are squares and multiples of 12. Which of the following is/are true?
 - I. A has infinitely many numbers.
 - II. A has a number whose sum of digits is 9.
 - III. A has a number whose sum of digits is 18.
 - $(A) I \ only \qquad (B) \ II \ only \qquad (C) \ III \ only \qquad (D) \ II \ and \ III \ only \qquad (E) \ All$
- 29. If a sequence of numbers $a_1, a_2, a_3,...$ is given by $a_{n+1} = \frac{1}{2-a_n}$ for n > 1 and $a_1 = \frac{1}{4}$, then the value of a_{2019} is
 - (A) $\frac{1}{4}$ (B) $\frac{4}{7}$ (C) $\frac{3}{4}$ (D) $\frac{6055}{6058}$ (E) $\frac{6058}{6061}$

30. In the following addition problem, different letters take different digits but none of them takes 8.

What is the sum of the digits of the maximum number SUPER can take?

- (A) 15
- (B) 16
- (C) 17
- (D) 18
- (E) 19

Thank you very much for your participation in the Sri Lankan Mathematics Competition SLMC 13 - 2019. Your score on this competition will be posted against your index number in www.slmathsolympiad.org. In this competition we have tried to showcase mathematics by posing puzzle type problems covering various areas of mathematics. Though the problems require very little knowledge of mathematics, not more than a Year 6 student's basic mathematics knowledge, some problems might require the mathematical maturity of a student in a higher grade. We hope that this kind of problems will stimulate your interest in mathematics beyond classroom mathematics. If you didn't do too well, don't be discouraged! You may have great mathematical talent, but it requires nurturing!! You have to learn problem solving strategies. Solve math problems for fun. Doing mathematics outside the school curriculum box will greatly improve your school mathematics.

As you know doing these problems in the exam hall under the pressure of time is difficult. This way may not bring the best in you. We hope that you will leisurely do and think about these problems after the competition. Looking back at the problems you solved and reflecting on them will improve your mathematical thinking. Some of these problems have deep mathematical ideas in them. History shows us that some mathematical ideas we have to learn in school evolved through long periods of time baffling the greatest mathematical minds in those times. For example negative numbers. Leo Rogers says at http://nrich.maths.org/5961:

"Although the first set of rules for dealing with negative numbers was stated in the 7th century by the Indian mathematician Brahmagupta, it is surprising that in 1758 the British mathematician Francis Maseres was claiming that negative numbers "... darken the very whole doctrines of the equations and make dark of the things which are in their nature excessively obvious and simple".

Read that article. Mathematics is a beautiful subject. But to see the beauty you have to engage in good mathematics. We hope that this competition will help you to see the beauty in mathematics.

For any comments/suggestions: <u>info@slmathsolympiad.org</u>

